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## Submonolayer Nucleation in Ultrathin Liquid Films: Scaling Properties and the Effects of the Critical Nucleus Size

Haley Doran  
*Western Washinton University*

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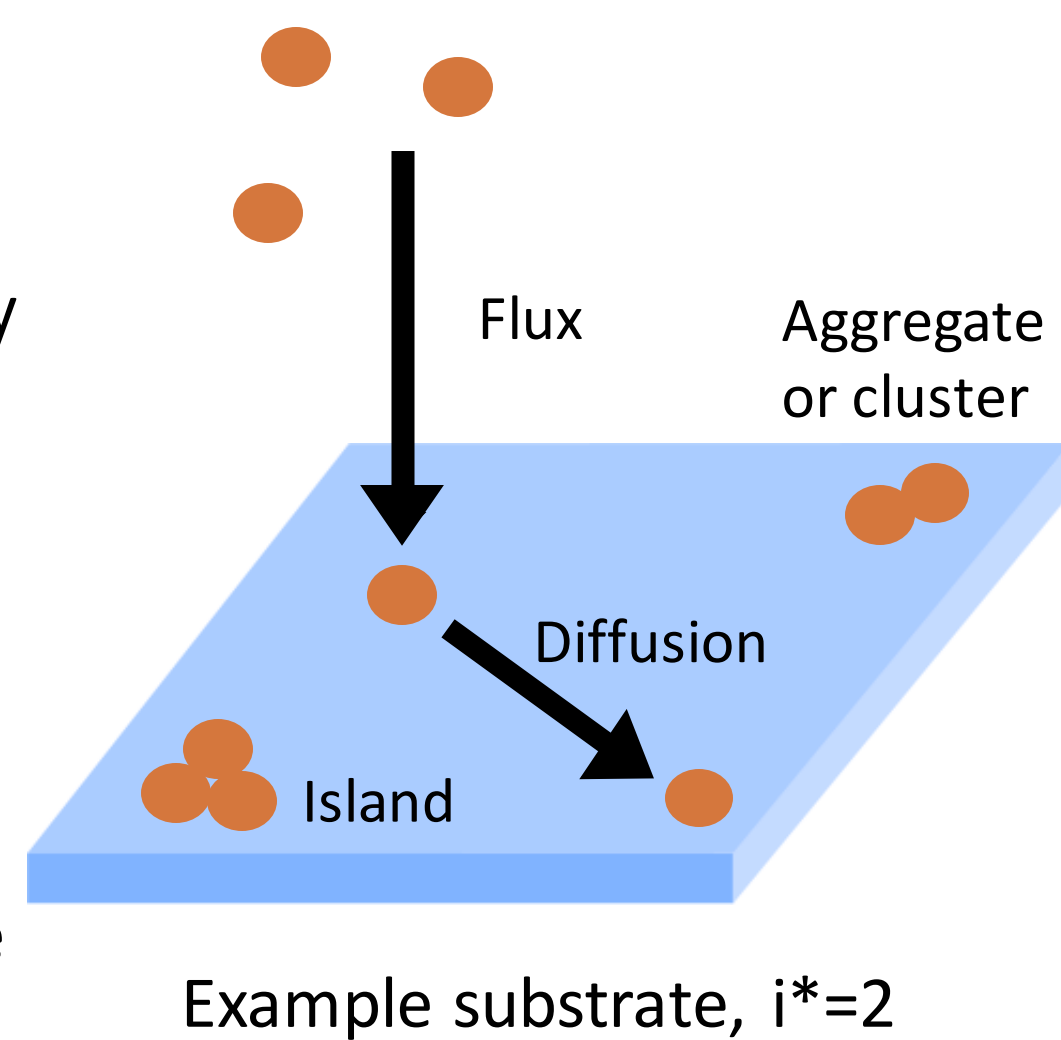
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# Submonolayer Nucleation in Ultrathin Liquid Films: Scaling Properties and the Effects of the Critical Nucleus Size

Haley J. Doran, Dr. David Patrick, Dr. Brad Johnson, Department of Chemistry, Western Washington University

## Background

- The system modeled by all approaches discussed here consists of a substrate that monomers (molecules or atoms) are fluxed onto at a constant rate  $F$
- Monomers may move around and aggregate with other monomers, forming a cluster or stable island, but may not leave the substrate
- A stable island is formed when a cluster has one more monomer than the critical cluster size,  $i^*$
- A predominant approach to modeling these systems is via kinetic Monte Carlo (KMC) simulation; however, they are computationally expensive for large  $i^*$  systems
- Mean free rate equation (MFRE) models consist of simple rate laws and are computationally inexpensive, but average over microscopic details that may be important
- Our novel multiscale model (MM) can achieve large  $i^*$  systems without losing this detail



## Our Goal

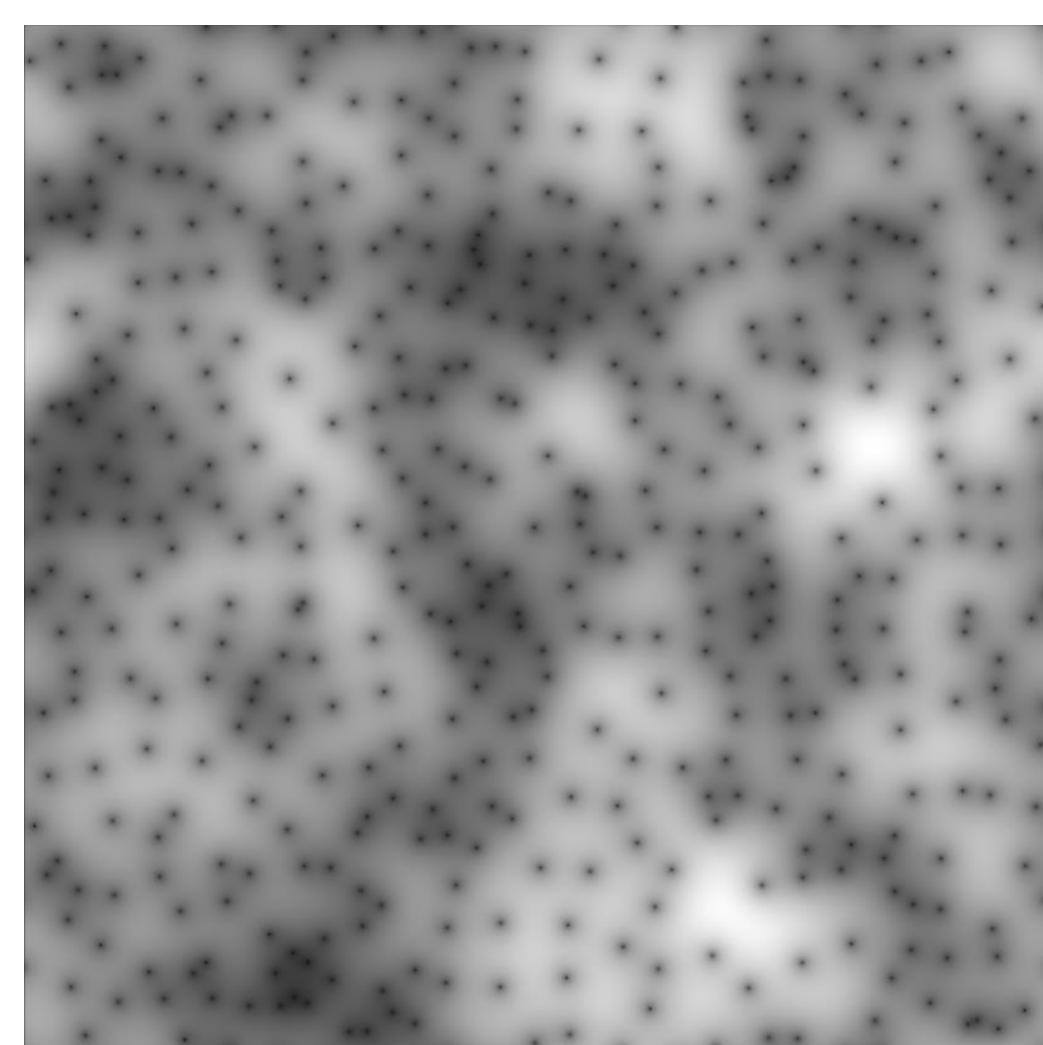
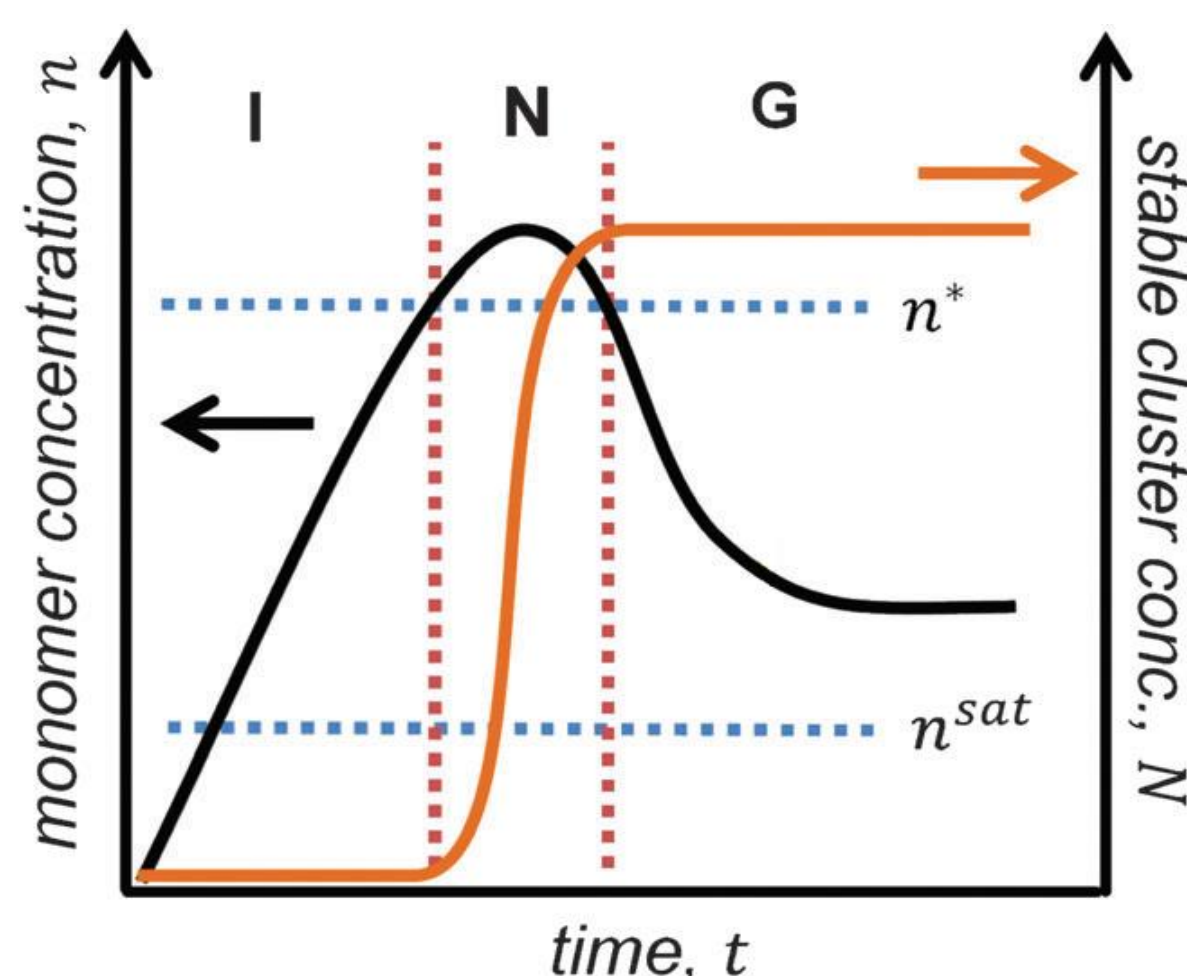
Submonolayer nucleation and growth in vacuum-deposited films are well described by KMC models due to their small critical cluster sizes. However, systems with large  $i^*$  values, such as those that occur during solution-phase nucleation, remain unexplored. Such systems are of particular interest for the fundamental understanding of the physics behind the growth of large, low-defect organic crystals via organic-vapor-liquid-solid deposition, which have novel semiconductor applications. Additionally, the MM is built on physical principals alone, while others have more empirical approaches; how will their behavior compare, and will these small  $i^*$  intended models be able to scale large  $i^*$  systems?

## The Multiscale Model

- The MM simulates a burst nucleation regime under a classical nucleation theory approach
- The MM includes a self-consistent treatment of  $i^*$  that is integrated into a mean field approach, stochastic treatment of nucleation, and analytically calculated monomer diffusion via the 2D diffusion equation
- BN consists of phases and can be represented by couples rate equations
  - Induction:** constant flux of monomers with no nucleation
  - Nucleation:** critical concentration  $n^*$  is reached and nucleation begins
  - Growth:** monomers are more likely to join an island than aggregate with monomers, there is no nucleation and only island growth
- Nucleation is periodically checked at every grid space by weighing the probability of nucleation, based on  $P(i^*, n)$ , against a random number generator
- The end result is a 2D landscape where each grid space represents the monomer concentration at that location
- Areas of lower monomer concentration are lighter and areas of greater concentration are darker
- Islands are likely to be found in the centers dark circles, due to their behavior as monomer sinks

$$\frac{\partial N}{\partial t} = KP(i^*, n)n$$

$$\frac{\partial n}{\partial t} = F - KP(i^*, n)n - KnN$$



$N$  = supercritical stable cluster conce.  
 $n$  = subcritical cluster conce.  
 $K$  = collisions and capture kernel  
 $P(i^*, n)$  = conce. of aggregates with monomer conc.  $n$  and size  $i^*$   
 $F$  = flux

## Scaling Models

### Mulheran & Blackman's Semiempirical Model

$$F(s) = \left[ \frac{\alpha^\alpha}{\Gamma(\alpha)} \right] s^{\alpha-1} \exp(-\alpha s)$$

$\alpha$  is a normalizing constant

- Scales size distributions for Voronoi cell areas where  $s$ =cell size/average cell size
- Based on a model from a computational analytical experiment consisting of randomly dispersed particles, assigning Voronoi cells, and generating the above distribution from the outputs

### Pimpinelli & Einstein's Wigner Surmise Application

$$P_\beta(s) = a_\beta s^\beta \exp(-b_\beta s^2)$$

$a_\beta$  and  $b_\beta$  are normalizing constants

- An approximation that describes spacing statistics that is derived from random matrix theory

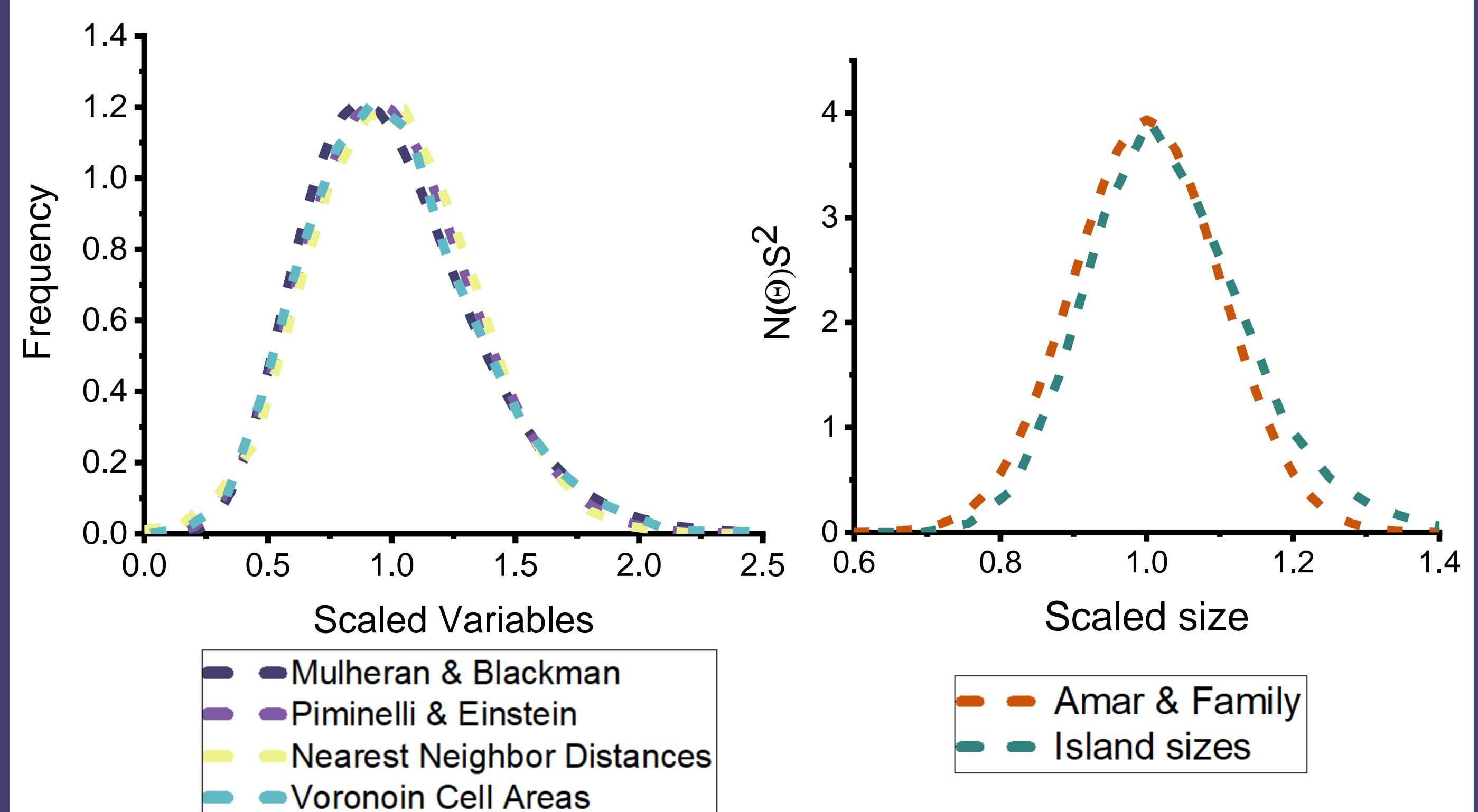
### Amar & Family's General Scaling Form:

$$f(u) = C_i u^i \exp(-ia_i u^{1/a_i})$$

$C_i$  and  $a_i$  are normalizing constants

- A general scaling form applied by Amar and Family to determine critical island sizes in physical experiments where iron is deposited onto iron and copper substrates
- Relates critical island size to island size scaling

## Comparative Model Analysis



- Both Mulheran & Blackman and Pimpinelli & Einstein approaches agree very well with the multiscale model's nearest neighbor and Voronoi cell area distributions
- This suggests that these scaling forms hold true in large  $i^*$  systems
- The Amar & Family fit predicts an  $i^*$  of 38, where the multiscale model calculated an  $i^*$  of 57 for the parameters run (Note  $\theta$  is coverage and  $S$  is avg. island size)
- Although the parameters scaling these models to the multiscale models' behavior do not have direct meaning in the large  $i^*$  regime, the fact that the curves themselves fit show that these fundamental models don't disagree with the multiscale model
- The scaling agreements also prove that such a simple, computationally inexpensive model can provide accurate scaling behavior

## References

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